

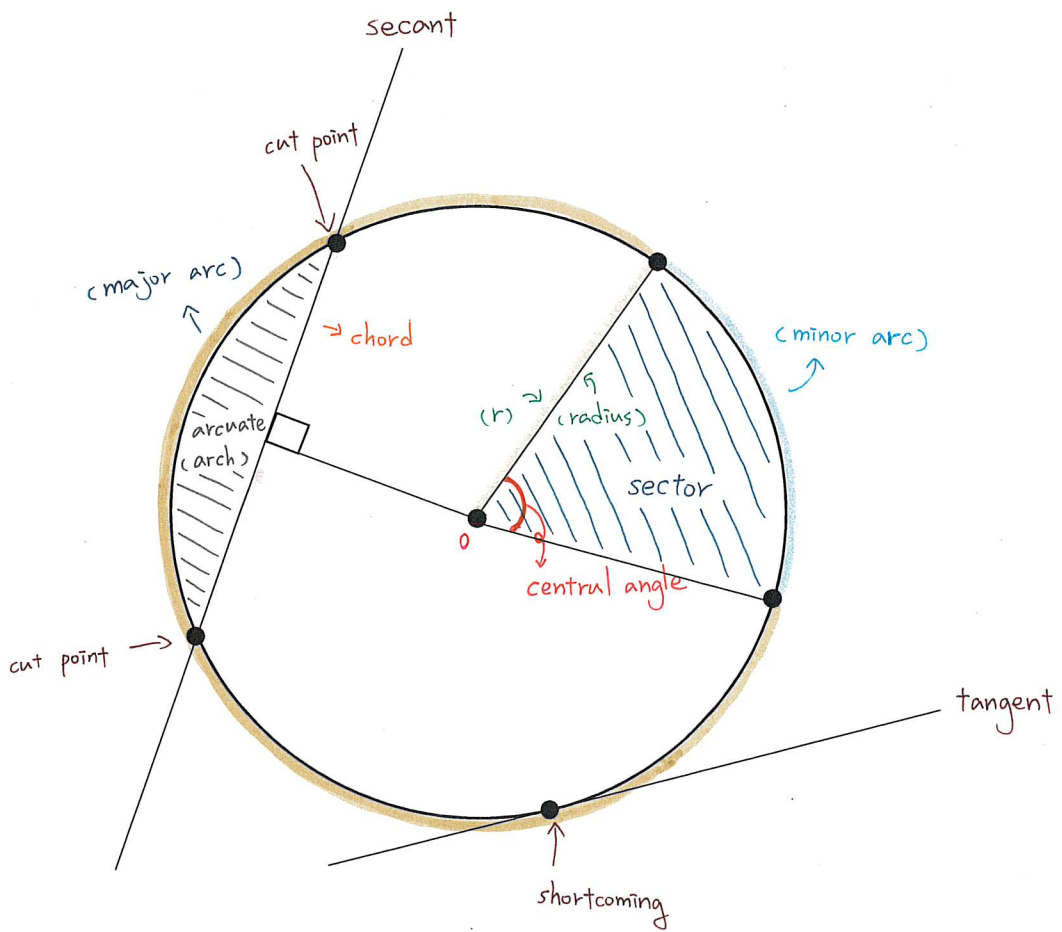
單元名稱 Basic concept of circle 圓形基本概念

● Definition the circle 圓的定義

1. The circle is a shape.

Consisting of all points in a plane that are at a given distance  $\downarrow$  radius (r)  
from a given point.  $\downarrow$  center of the circle (o)

● The names of various parts of the circle 圓各部位的名稱

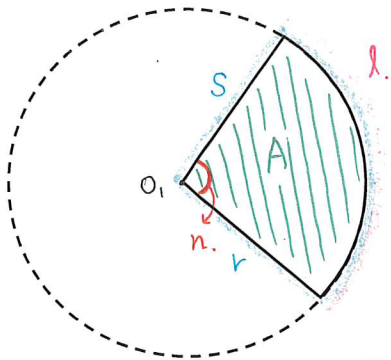


單元名稱

The area and perimeter of sectors and arcuates 扇形、弓形的面積與周長

● The area and perimeter of sectors

面積



The area of a sector  
= The area of a circle  $\times$  ratio (比例)

$$\text{ratio} = \frac{\text{center angle (圓心角)}}{\text{inscribed angle (周角 = } 360^\circ)}$$

$$\text{or ratio} = \frac{\text{arc length (被加數)}}{\text{circumference (圓周長)}}$$

A = 面積  
S = 周長  
r = 半徑  
l = 弧

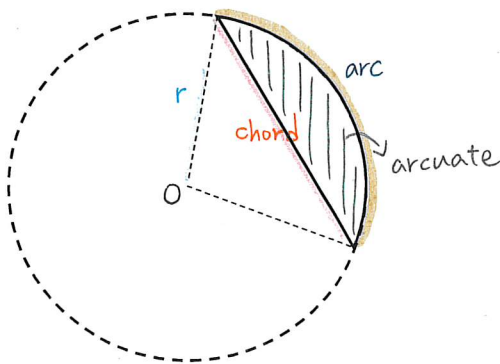
$$A = r^2 \pi \times \frac{n}{360}$$

$$= r^2 \pi \times \frac{l}{2r\pi} = \frac{r \times l}{2}$$

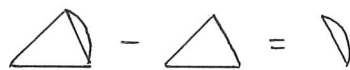
周長  
The perimeter of a sector  
= the arc length + diameter (直徑)  
the arc length = the circumference  $\times$  ratio

$$S = 2r\pi \times \frac{n}{360} + 2r$$

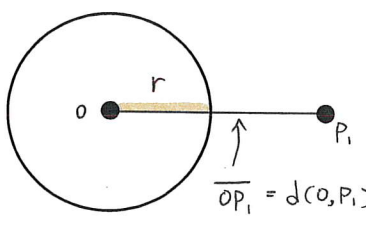
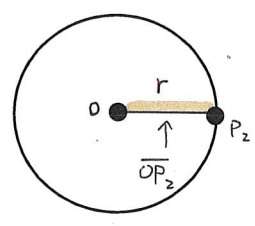
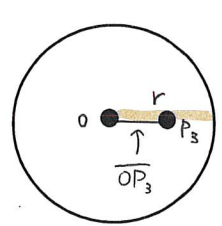
● The area and perimeter of arcuates

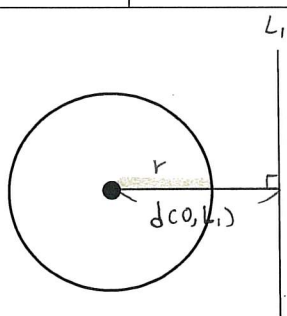
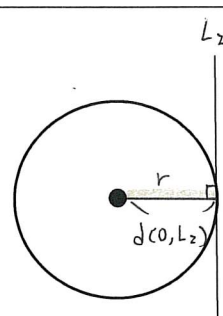
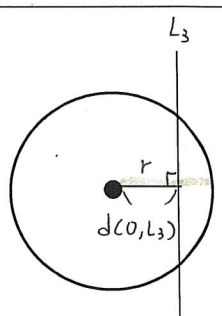


The area of arcuate  
= The area of a sector  
= The area of a triangle



The perimeter of a arcuate  
= the arc length + the chord length

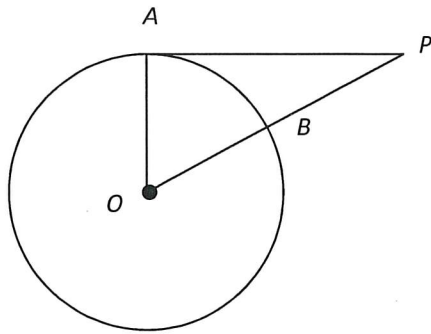
單元名稱	The relative position of a circle and a point 點與圓的相對位置關係	
 <p>(If) <math>\overline{OP}_1 &gt; r</math>  <math>\rightarrow P_1 \in \text{outer}</math></p>	 <p>(If) <math>\overline{OP}_2 = r</math>  <math>\rightarrow P_2 \in \text{on}</math></p>	 <p>(If) <math>\overline{OP}_3 &lt; r</math>  <math>\rightarrow P_3 \in \text{inner}</math></p>

單元名稱	The relative position of a circle and a line 點與線的相對位置關係	
 <p>(If) <math>d(O, L_1) &gt; r</math>  <math>\rightarrow L_1 \in \text{none intersection point}</math></p>	 <p>(If) <math>d(O, L_2) = r</math>  <math>\rightarrow L_2 \in \text{tangent}</math>  <math>\Rightarrow \text{a intersection point}</math></p>	 <p>(If) <math>d(O, L_3) &lt; r</math>  <math>\rightarrow L_3 \in \text{secant}</math>  <math>\Rightarrow \text{two intersection points}</math></p>

單元名稱

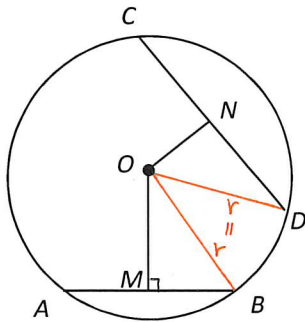
Calculate the segments of a tangent and the chord length  
計算切線段長與弦長

- Calculate the segments of a tangent



$$d(O, P)^2 = (\text{radius})^2 + (\text{the } \textit{\text{線段}} \text{ segments of a tangent})^2$$

- Calculate the chord length



$$(\text{radius})^2 = d(O, \text{chord})^2 + \frac{(\text{the chord length})^2}{2}$$

$$\begin{aligned} * \text{ if } \overline{OM} > \overline{ON} \\ \rightarrow \overline{AB} < \overline{CD} \end{aligned}$$

單元名稱

Basic concept of circle 圓形基本概念

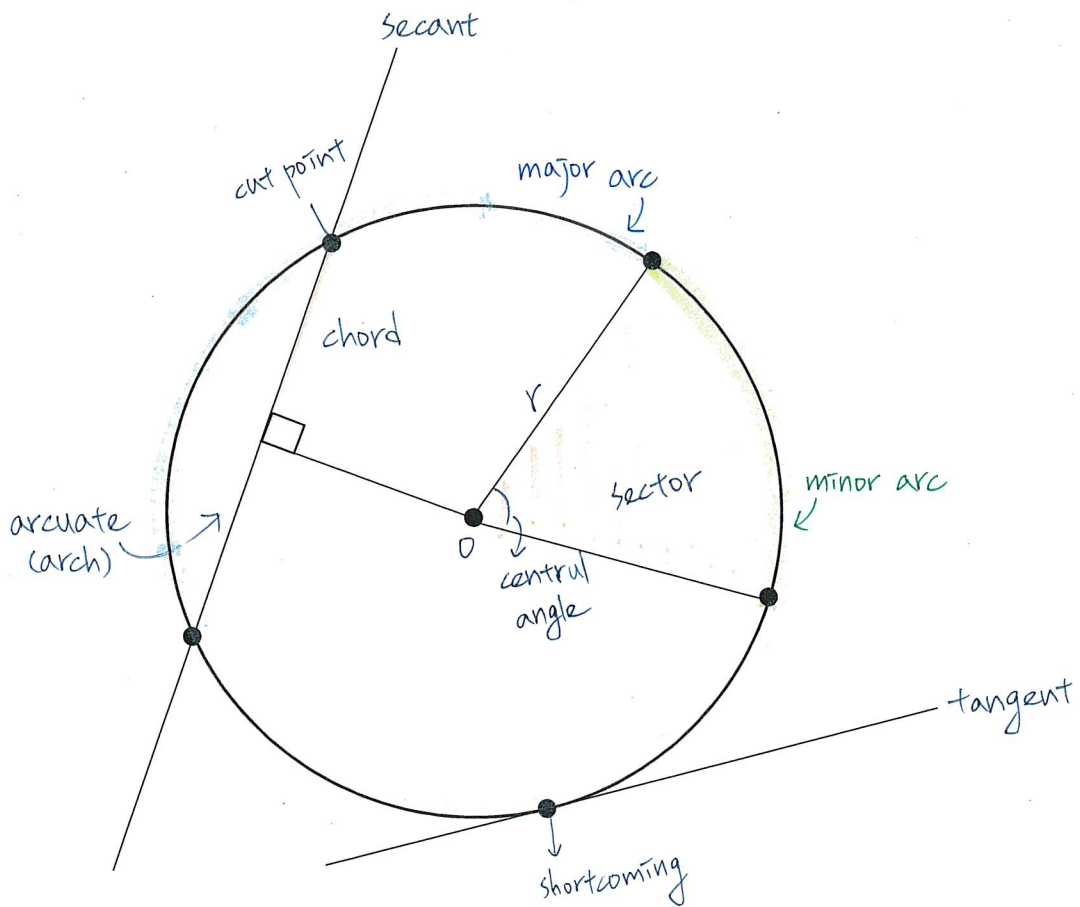
● Definition the circle 圓的定義

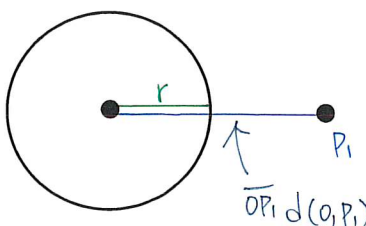
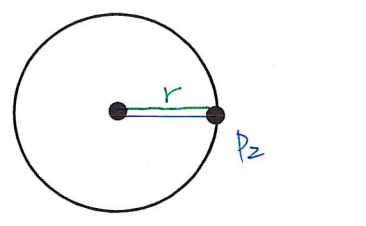
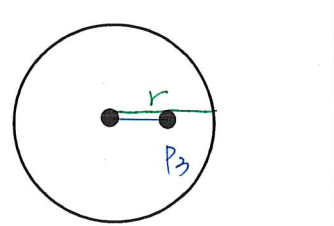
A circle is a shape consisting of all points in a plane that are at a given distance from a given point.

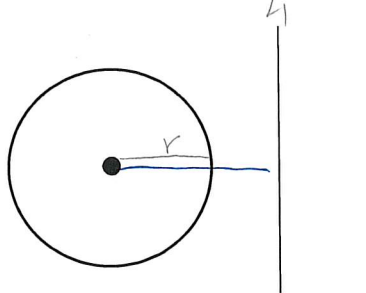
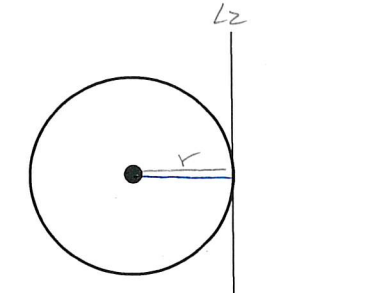
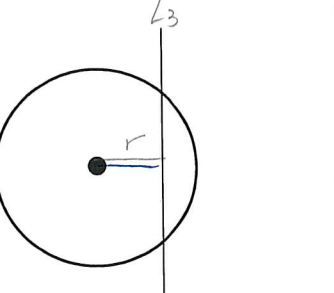
radius( $r$ )

center of the circle  
( $O$ )

● The names of various parts of the circle 圓各部位的名稱



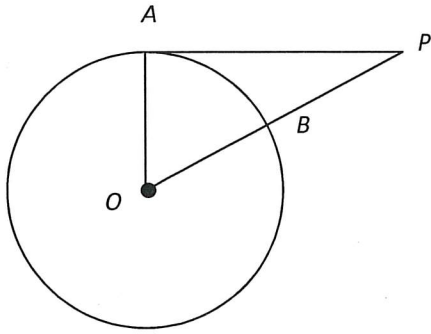
單元名稱	The relative position of a circle and a point 點與圓的相對位置關係 關係 位置	
 <p data-bbox="223 672 590 761">if <math>\overline{OP_1} &gt; r \rightarrow P_1 \in \text{outer}</math> 則</p>	 <p data-bbox="670 672 1037 761">if <math>\overline{OP_2} = r \rightarrow P_2 \in \text{on}</math></p>	 <p data-bbox="1149 672 1484 761">if <math>\overline{OP_3} &lt; r \rightarrow P_3 \in \text{inner}</math></p>

單元名稱	The relative position of a circle and a line 點與線的相對位置關係	
 <p data-bbox="159 1411 590 1612">if <math>d(O, L_1) &gt; r \rightarrow L_1 \in \text{no}</math> intersection point</p>	 <p data-bbox="606 1411 1037 1568">if <math>d(O, L_2) = r \rightarrow L_2 \in \text{tangent} \Rightarrow 1</math> intersection point</p>	 <p data-bbox="1053 1411 1484 1635">if <math>d(O, L_3) &lt; r \rightarrow L_3 \in \text{secant} \Rightarrow 2</math> intersection points</p>

單元名稱

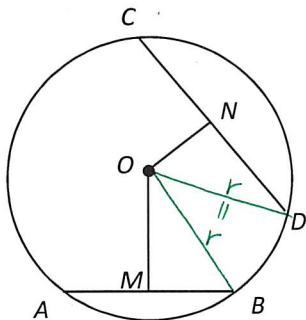
Calculate the segments of a tangent and the chord length  
計算切線段長與弦長

● Calculate the segments of a tangent



$$d(o,p)^2 = (\text{radius})^2 + (\text{the } \text{線段} \text{ segments of a tangent})^2$$

● Calculate the chord length



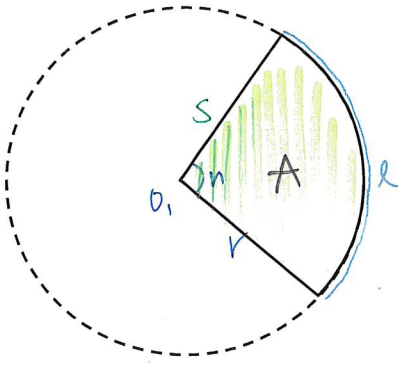
$$(\text{radius})^2 = d(o, \text{chord})^2 + (\text{the chord length}/2)^2$$

\* if  $OM > ON \rightarrow AB < CD$

單元名稱

The area and perimeter of sectors and arcuates 扇形、弓形的面積與周長

● The area and perimeter of sectors



The area of a <sup>扇形</sup> sector = The area of a circle \* <sup>比例</sup> ratio  
 ratio = <sup>圓心角</sup> center angle / <sup>周角=360°</sup> inscribed angle

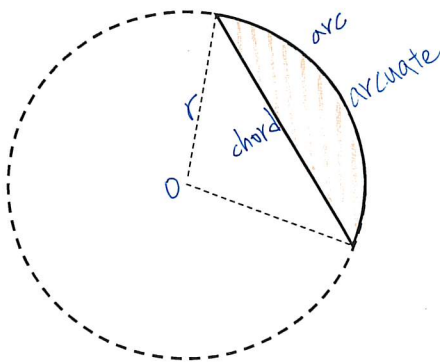
or ratio = arc length / <sup>圓周長</sup> circumference

$$A = r^2 \pi \times \frac{n}{360} = r^2 \pi \times \frac{l}{2r\pi} = \frac{r \times l}{2}$$

The <sup>周長</sup> perimeter of a sector = the arc length + <sup>直徑</sup> diameter  
 the arc length = the circumference \* ratio

● The area and perimeter of arcuates

$$S = 2r\pi \times \frac{n}{360} + 2r$$



The area of a arcuate:  
 = The area of a sector - The area of a triangle

The perimeter of a arcuate  
 = the arc length + the chord length



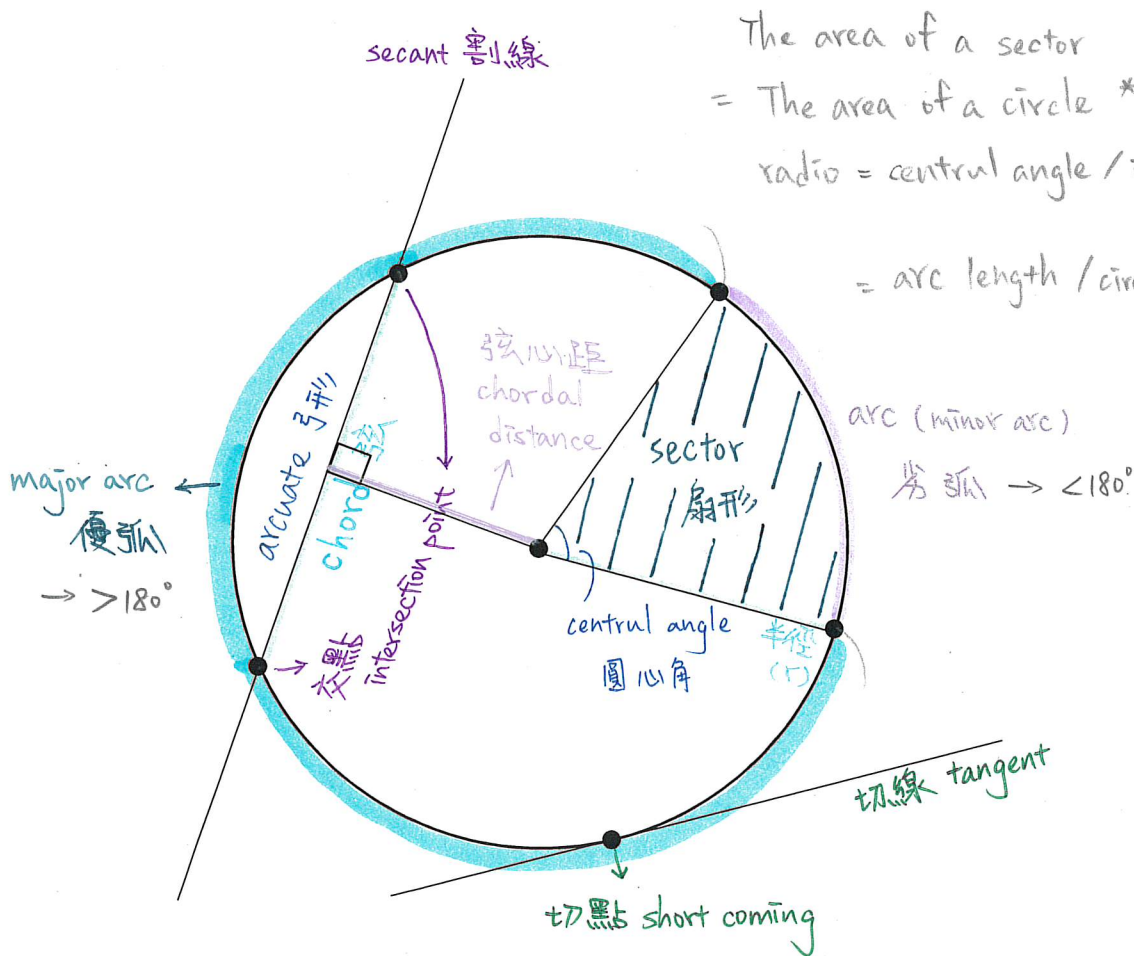
單元名稱 Basic concept of circle 圓形基本概念

● Definition the circle 圓的定義

A circle is a shape consisting of all the points in a plane that are at a given distance from a given point.

radius (r)                      the center of circle

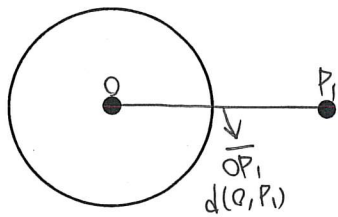
● The names of various parts of the circle 圓各部位的名稱



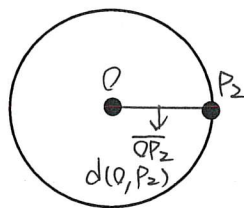
The area of a sector  
 = The area of a circle \* radio (radius)  
 radio = central angle / inscribed angle  
 (周角 = 360°)  
 = arc length / circumference

area of the circle =  $r^2 \pi$   
 circumference =  $2r$  (diameter)  $\times \pi$

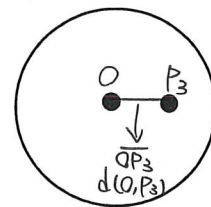
單元名稱	The relative position of a circle and a point <span style="margin-left: 20px;">關係 位置</span> 點與圓的相對位置關係
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if  $\overline{OP_1} > r$   
 →  $P_1 \in \text{outer}$  圓外  
 則

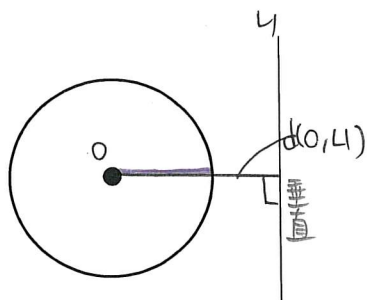


if  $\overline{OP_2} = r$   
 →  $P_2 \in \text{on}$  圓上

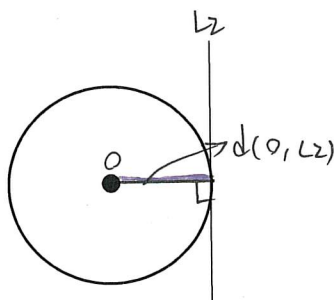


if  $\overline{OP_3} < r$   
 →  $P_3 \in \text{inner}$  圓內

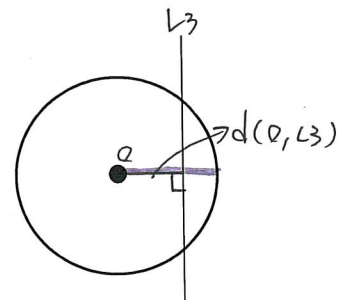
單元名稱	The relative position of a circle and a line <span style="margin-left: 20px;">點與線的相對位置關係</span>
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if  $d(O, L_1) > r$   
 $L_1 \in \text{nope}$  → intersection point  
 ↪ 沒有焦點



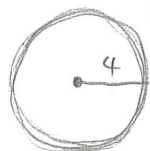
if  $d(O, L_2) = r$   
 $L_2 \in \text{tangent}$  切線  
 ↪ 一個焦點



if  $d(O, L_3) < r$   
 $L_3 \in \text{secant}$  割線  
 ↪ 兩個焦點

∈ = blown to 屬於

1. 已知圓  $O$  半徑為 4,  $A$ 、 $B$ 、 $C$  三點與圓心  $O$  的距離分別為 3、4、5, 判別  $A$ 、 $B$ 、 $C$  三點與圓  $O$  的位置關係。(圓外、圓上或圓內)



$$PA < 4$$

$$PB = 4$$

$$PC > 4$$

$$A = \begin{matrix} \text{外} = PC \\ \text{圓} \\ \text{上} = PB \\ \text{內} = PA \end{matrix}$$

2. 已知圓  $O$  半徑為 5,  $A$ 、 $B$ 、 $C$  三點與圓心  $O$  的距離分別為 6、5、4, 判別  $A$ 、 $B$ 、 $C$  三點與圓  $O$  的位置關係。(圓外、圓上或圓內)

$$PA > 5$$

$$PB = 5$$

$$PC < 5$$

$$A = \begin{matrix} \text{外} = PA \\ \text{圓} \\ \text{上} = PB \\ \text{內} = PC \end{matrix}$$

3. 已知圓  $O$  半徑為 6,  $A$ 、 $B$ 、 $C$ 、 $D$  四點與圓心  $O$  的距離分別為 10、8、6、2, 判別  $A$ 、 $B$ 、 $C$ 、 $D$  四點與圓  $O$  的位置關係。(圓外、圓上或圓內)

$$PA > 6$$

$$PB > 6$$

$$PC = 6$$

$$PD < 6$$

$$A = \begin{matrix} \text{外} = PA, PB \\ \text{圓} \\ \text{上} = PC \\ \text{內} = PD \end{matrix}$$

4. 已知圓  $O$  半徑為 8,  $A$ 、 $B$ 、 $C$ 、 $D$  四點與圓心  $O$  的距離分別為 9、8、7、5, 判別  $A$ 、 $B$ 、 $C$ 、 $D$  四點與圓  $O$  的位置關係。(圓外、圓上或圓內)

$$PA > 8$$

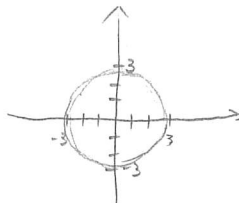
$$PB = 8$$

$$PC < 8$$

$$PD < 8$$

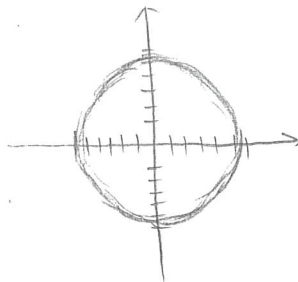
$$A = \begin{matrix} \text{外} = PA \\ \text{圓} \\ \text{上} = PB \\ \text{內} = PC, PD \end{matrix}$$

5. 在坐標平面上, 若以  $(0, 0)$  為圓心, 3 為半徑畫圓,  $A(0, -3)$ 、 $B(-3, -2)$ 、 $C(4, 2)$  三個點中, 哪幾個點在圓外?



$$A = C(4, 2)$$

6. 在坐標平面上, 若以  $(0, 0)$  為圓心, 6 為半徑畫圓, 則  $A(4, -3)$ 、 $B(-1, 5)$ 、 $D(-5, -4)$  三個點中, 哪幾個點在圓內?



$$A(4, -3)$$

$$A = B(-1, 5)$$

$$D(-5, -4)$$

7. 在坐標平面上, 若以  $(0, 0)$  為圓心, 10 為半徑畫圓, 則  $A(3, 4)$ 、 $B(6, -8)$ 、 $C(10, 0)$  三個點中, 哪幾個點在圓上?

$$A = C(10, 0)$$

8. 在坐標平面上, 若以  $(0, 0)$  為圓心, 13 為半徑畫圓, 則  $A(6, 3)$ 、 $B(-5, 12)$ 、 $C(2, -8)$ 、 $D(9, 10)$ 、 $E(0, -12)$  五個點中, 哪幾個點在圓內?

$$A(6, 3)$$

$$A = B(-5, 12)$$

$$C(2, -8)$$

$$D(9, 10)$$

$$E(0, -12)$$

1. 已知圓的半徑為 5，若三直線  $L_1$ 、 $L_2$ 、 $L_3$  分別與圓心的距離為 4、5、6，求此三直線與圓的交點個數。

$$\begin{aligned} L_1 &< 5 \\ L_2 &= 5 \\ L_3 &> 5 \end{aligned}$$

$$A = \begin{cases} L_1 = 0 \\ L_2 = 1 \\ L_3 = 2 \end{cases} \text{ 個}$$

2. 已知圓的半徑為 3.5，若三直線  $L_1$ 、 $L_2$ 、 $L_3$  分別與圓心的距離為 3、4、5，求此三直線與圓的交點個數。

$$\begin{aligned} L_1 &< 3.5 \text{ (V)} \\ L_2 &> 3.5 \\ L_3 &> 3.5 \end{aligned}$$

$$A = \begin{cases} L_1 = 2 \\ L_2 = 0 \\ L_3 = 0 \end{cases} \text{ 個}$$

3. 已知圓的直徑為 12，若三直線  $L_1$ 、 $L_2$ 、 $L_3$  分別與圓心的距離為 5、6、7，求此三直線與圓的交點個數。

$$\begin{aligned} r &= 6 \\ L_1 &< 6 \\ L_2 &= 6 \\ L_3 &> 6 \end{aligned}$$

$$A = \begin{cases} L_1 = 2 \\ L_2 = 1 \\ L_3 = 0 \end{cases} \text{ 個}$$

4. 已知圓的直徑為 10，若三直線  $L_1$ 、 $L_2$ 、 $L_3$  分別與圓心的距離為 3、4、5，求此三直線與圓的交點個數。

$$\begin{aligned} L_1 &< 5 \\ L_2 &< 5 \\ L_3 &= 5 \end{aligned}$$

$$A = \begin{cases} L_1 = 2 \\ L_2 = 2 \\ L_3 = 1 \end{cases} \text{ 個}$$

5. 已知圓的半徑為 6，若圓心  $O$  到三直線  $A$ 、 $B$ 、 $C$  的距離分別為 8、6、4，則哪一條是切線？哪一條是割線？

$$A = \begin{cases} \text{切} = \overline{OB} \\ \text{割} = \overline{OC} \end{cases}$$

6. 已知圓的半徑為 11，若圓心  $O$  到三直線  $P$ 、 $Q$ 、 $R$  的距離分別為 9、12、11，則哪一條是切線？哪一條是割線？

$$A = \begin{cases} \text{切} = \overline{OR} \\ \text{割} = \overline{OP} \end{cases}$$

7. 已知圓的直徑為 14，若圓心  $O$  到三直線  $A$ 、 $B$ 、 $C$  的距離分別為 5、7、9，則哪一條是切線？哪一條是割線？

$$A = \begin{cases} \text{切} = \overline{OB} \\ \text{割} = \overline{OA} \end{cases}$$

8. 已知圓的直徑為 20，若圓心  $O$  到三直線  $P$ 、 $Q$ 、 $R$  的距離分別為 16、9、10，則哪一條是切線？哪一條是割線？

$$A = \begin{cases} \text{切} = \overline{OR} \\ \text{割} = \overline{OQ} \end{cases}$$